

Scandium: A key element for understanding Am stars

F. LeBlanc¹ and G. Alecian²

¹ Département de Physique et d'Astronomie, Université de Moncton, Moncton, NB, E1A 3E9, Canada

² LUTH (Observatoire de Paris - CNRS), Observatoire de Meudon, 92195 Meudon Cedex, France

Received *date will be inserted by the editor* Accepted *date will be inserted by the editor*

Abstract. Context. Atomic diffusion is believed to cause the abundance anomalies observed in AmFm stars. However, the detailed process has still not been well-established. For instance, two possible scenarios for the diffusion theory are presently envisaged. They differ mainly by the depth from which the abundance anomalies emanate. The first scenario predicts that the abundances are modified in the superficial regions of the star, just below the hydrogen convection zone. The second scenario predicts that a much deeper extension of the mixing zone exists due to the convection caused by Fe accumulation in regions below the hydrogen convection zone.

Aims. We calculate much more accurate radiative accelerations of Sc than previously, to better understand the observed abundance anomalies of this element. We believe that it is a key element to use as a diagnostic tool for understanding AmFm stars.

Methods. The method employed to obtain these radiative accelerations is based on an interpolation from the parameters of the so-called SVP parametric method.

Results. The radiative accelerations, shown here in a typical Am stellar model, are discussed in light of the observed anomalies of Ca and Sc. Our results suggest that the deeper mixing scenario is not entirely satisfactory: the mixing zone should be deeper than what is predicted by recent models to account for observed Sc underabundances. Our results seem more compatible with the scenario where the abundances anomalies are created in the superficial regions. However, only detailed evolutionary modelling with mass loss and diffusion of all important species, including Ca and Sc, with accurate radiative accelerations, will be able to give more insight into where the source of these anomalies occur in AmFm stars.

Key words. diffusion – stars: abundances – stars: chemically peculiar

1. Introduction

Among the main observational peculiarities of Am stars are the superficial underabundances of Ca and Sc, as well as an overabundance of iron-peak elements (e.g. Preston 1974). The classical explanation of the AmFm star phenomenon is that these stars, which are slow rotators, are supposed to have smaller large-scale (mixing) motions in their envelope than *normal* main sequence stars. Since these stars are almost always in binary systems, their slow rotation is believed to be due to tidal forces (Abt 1961). The relative stability of their envelope allows for a large proportion of He atoms to sink towards the deeper regions due to gravitational settling, leading to the disappearance of the He convection zone. The abundance anomalies were then thought to be produced by the diffusion process (Michaud 1970) at the bottom of the hydrogen convection zone (Watson 1971, Smith 1971, Michaud et al. 1983, Alecian 1996). At that depth, Ca is mostly

in its Ar-like configuration so its radiative acceleration is weak because of its noble gas configuration, thus leading to its underabundance in the superficial hydrogen convection zone. The radiative acceleration (g_{rad}) is due to the momentum transfer from photons to atoms during photoabsorption. The value of g_{rad} of a given element depends on its absorption cross-section, on its abundance and on the local physical conditions of the plasma (e.g. Alecian & LeBlanc 2000). The diffusion process that can create over or underabundances at various depths is a non linear, time-dependent process that can affect the structure and the evolution of stars.

Numerical modelling of Ca and Sc time-dependent diffusion in AmFm stars was carried out by Alecian (1996). This modelling corresponds to the scenario first proposed by Watson (1971), but including a bulk velocity due to mass loss (as considered for λ Bootis stars by Michaud & Charland 1986). Superficial abundances of these elements appear to depend closely on the age of the star, on the mass loss rate, and they are very sensitive to the position of the bottom of the superficial mixing zone (hy-

drogen convection zone plus overshooting). In these computations, the stellar model was static and no structure evolution was considered (the star was kept at the same position on the main sequence), only diffusion was time-dependent.

Recent evolutionary models including the effect of the diffusion of the elements show that a Fe convection zone can occur due to its accumulation at certain depths (Richard, Michaud & Richer 2001 and Richer, Michaud & Turcotte 2000), and suggest that the abundance anomalies emanate from deeper layers (at temperatures of approximately 200 000 K). At that depth, a large proportion of Ca is also in a noble gas configuration (Ne-like) which explains its observed underabundance. However, these computations are done without mass loss. Mass loss has two effects: it smooths the abundance inhomogeneities, and it shifts the abundance stratifications produced by diffusion towards shallower layers in the star (Michaud & Charland 1986; Alecian 1996). Therefore, mass loss may affect iron accumulation and thus the Fe convection zone predicted by these evolutionary models.

The study of Ca diffusion is relatively easy because its atomic data are rather well known. Indeed, a good knowledge of the atomic data is essential since radiative accelerations are, with gravity, among the main ingredients in the diffusion equation. The situation for Sc is quite different. For instance, both the OPAL opacities (e.g. Rogers & Iglesias 1992) and the Opacity Project (hereafter OP, Seaton et al. 1992) do not include scandium in their databases. The Kurucz (1990) data include only the first nine Sc ions. The detailed study of Sc diffusion has never been done. Alecian (1996) calculated the g_{rad} of Sc based on the parametric method of Alecian & Artru (1990a,b). But, as mentioned in his study, the calculated g_{rad} are not accurate enough since extrapolations had to be done to complete the data for highly ionized Sc ions. In this paper, we aim to calculate the g_{rad} of Sc by an interpolation method based on the parametric form of the g_{rad} formulae of Alecian & LeBlanc (2002) and LeBlanc & Alecian (2004) (hereafter respectively Papers I and II).

Because scandium underabundance, along with the one of calcium, characterizes AmFm stars, it is a key element to better understand the AmFm phenomenon. Scandium is in an ionisation state with noble gas configuration in layers close to the bottom of the H convection zone, and close to the bottom of the Fe convection zone predicted by Richer, Michaud & Turcotte (2000), but not at the same positions as for the corresponding calcium configurations. Any model of AmFm stars should be able to explain underabundances for both elements. Therefore, the study of Sc diffusion could possibly shed light on which one of the two diffusion scenarios, diffusion below the H convection zone while including mass loss (Alecian 1996; hereafter *scenario A*), and diffusion below the Fe convection zone (Richer, Michaud & Turcotte 2000; hereafter *scenario B*), is more likely to explain the abundance anomalies of these stars.

In Sec. 2, we present g_{rad} calculations for Sc while using an interpolation method related to the new parametric formulae described in Papers I and II. In Sec. 3, we discuss our g_{rad} with respect to the observed abundance anomalies of Ca and Sc in AmFm stars. A short conclusion follows.

2. Radiative acceleration calculations

2.1. Method used for g_{rad} calculations

Recently, an improved parametric method for calculating g_{rad} at large optical depths was developed (Papers I and II). The improvements, as compared to the method of Alecian & Artru (1990a,b), were made possible because of the use of OP opacities and data (Seaton et al. 1992). Once the parameters of the various ions are calculated, the parametric method has the advantage of giving relatively accurate g_{rad} without having to deal with the enormous amount of atomic data normally necessary to obtain g_{rad} . The parameters for 12 trace elements (C, N, O, Ne, Na, Mg, Al, Si, S, Ar, Ca and Fe) were calculated in Paper II.

The method used here to calculate the g_{rad} of Sc is based on this parametric form of g_{rad} formulae (SVP method) of both bound-bound (Alecian 1985, Alecian & Artru 1990a, Papers I and II) and bound-free (Alecian 1994, Papers I and II) transitions. In this method, radiative accelerations due to atomic lines depend on 4 parameters for each ion (Eq. (1) of Paper II), calculated at layers where the relative population of the ion i is near its maximum. The first parameter ϕ_i^* (Eqs. (10) to (13) of Paper I) is related to the strength of the bound-bound transitions through a weighted average of the gf values. The second parameter ψ_i^* (see Eq. (14) of Paper I) is related to the average width of the line profiles and controls saturation. A third parameter ξ_i^* is related to the ion contribution to the total opacity (we will neglect it for Sc since it is of little importance for less abundant elements). Meanwhile, the value of the parameter α_i ¹ is determined by fitting our parametric accelerations to those obtained by a more accurate method (Seaton 1997, see Paper I for more details).

A similar parametric equation was also used for bound-free transitions (Eq. (9) of Paper II). This approximate formula is less accurate than for bound-bound transitions and needs the knowledge of energy levels for each ion and the computation of the partition functions at each model layer. Two other parameters a_i and b_i (correction parameters for bound-free acceleration) are determined for each ion by a same kind of fitting procedure as employed for lines. These six parameters, along with the formulae of Paper II, define the SVP method. They are calculated here, in an Am stellar model, for the 12 trace elements mentioned above. These elements are treated by Seaton

¹ This parameter characterizes an average Voigt profile of the lines for the ion under consideration, see Eq. (1) of Paper II.

(1997), and our fitting procedure is achieved using version OPCD 2.1 of the tables available at CDS².

The accurate evaluation of radiative accelerations necessitates detailed and complete atomic data (including all strong transitions) for each element. This is still lacking for scandium. A rather large data base for energy levels can be found in the NIST Atomic Spectra Database³, but this database is incomplete for bound-bound transitions, especially in regards to transition probabilities.

As shown in Alecian & Artru (1990b), parameters ϕ_i^* and ψ_i^* generally vary quite monotonously along isoelectronic sequences. It is then possible to approximate these parameters for some of the ions of the elements for which atomic data are lacking, by interpolating between the nearest isoelectronic neighbours with known parameters, to the ions in question. The interpolation is done via the atomic charge variable. We have then considered that to apply this interpolation method to Sc ions, using well calculated parameters from isoelectronic neighbours, is preferable than to calculate directly the parameters, using incomplete atomic data. Also, it would be impossible to do the fitting procedure of Paper II, since the g_{rad} of Sc are not included in Seaton (1997) or elsewhere.

We have interpolated the parameters for the bound-bound transitions of the ions ScIII to ScXX, but not for ScII since parameters for an isoelectronic neighbour are missing (namely the parameters for CaI). The parameters which were directly evaluated by Alecian & Artru (1990b) for ScII from atomic data were then used. Parameters a_i and b_i were respectively set to 1 and 0 (this corresponds to no correction). Relative populations of Sc ions and partition functions have been calculated using the atomic energy level data of the NIST Atomic Spectra Database.

2.2. Numerical results

The results shown in this section have been obtained for a $1.9 M_{\odot}$ stellar model with $T_{\text{eff}} = 7610$ K and an age of 807 Myr (model named 1.9P1 in Talon, Richard & Michaud 2006).

To verify the accuracy of this interpolation method along isoelectronics sequences, we have simulated it for elements for which the parameters are obtained by detailed computations, and for which the SVP method is known to work well, i.e. Si and Ca (see Paper II). Note that for these elements, accurate radiative accelerations can also be calculated by the Seaton (1997) method, which makes the verification process especially confident. We have compared for these elements, accelerations obtained using their *true* parameters with those (assuming that they are unknown) obtained with parameters calculated by interpolation along isoelectronics sequences. Results confirmed the validity of our interpolation method, at least for Si and Ca (see Fig. 1). The parameters of some weakly ionized ions cannot be obtained by interpolation since they

do not have isoelectronic neighbours with known parameters. In order to include a maximum number of ions, we have used the parameters ϕ_i^* and ψ_i^* of SiII, CaII and CaIII from Alecian & Artru (1990b). The results for Ca are not very accurate at low temperatures. This is due to the fact that the parameters ϕ_i^* do not, in this case, vary monotonously for weakly ionized ions (see the figures in Alecian & Artru, 1990b). The interpolation method underestimates contributions of CaIV and CaV to the acceleration. Nevertheless, deeper in the star, both methods give very similar results. Although we only study the case of Sc in this work, we consider that this interpolation method could be extended to other elements for which the atomic data are not completely known, provided that their ions have isoelectronic neighbours for which parameters are well determined.

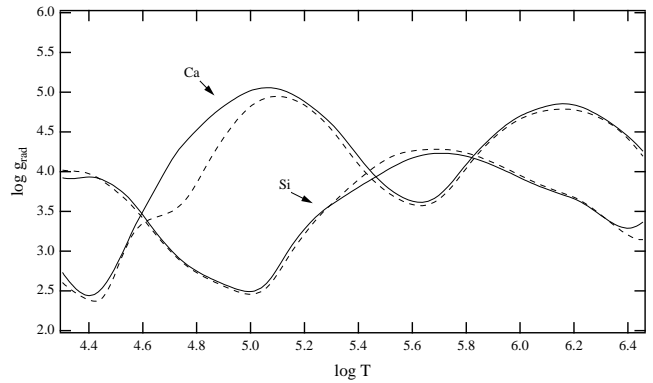


Fig. 1. Radiative accelerations of Si and Ca in a model with $T_{\text{eff}} = 7610$ K ($1.9 M_{\odot}$). The solid lines represent the results of the SVP method using known parameters, while the dashed lines represent the g_{rad} using the parameters obtained by our interpolation method.

Figure 2 shows the Ca and Fe radiative accelerations for a solar abundance using the SVP method and those obtained by applying the method of Seaton (1997)⁴. Also shown, are the g_{rad} found by Talon, Richard & Michaud (2006)⁵. These g_{rad} are calculated via the opacity sampling method (e.g. LeBlanc, Michaud & Richer 2000) using the local abundance obtained by the diffusion process. We may conclude, from these, that the results from the SVP method are satisfactory.

Figure 3 shows the g_{rad} of Sc (calculated by the interpolation method) and Ca (calculated by the SVP method). The parameters for Ca are the same as those used for the accelerations shown in Fig.2. The parameters for Sc are interpolated from those of Ca and Fe. Two abundances are shown: 1 and 0.1 times their solar values. The two valleys seen in the curves presented are related

² <http://vizier.u-strasbg.fr/topbase/op.html>

³ <http://physics.nist.gov/PhysRefData/ASD/index.html>

⁴ With version OPCD 2.1 of data and codes available at Centre de Données de Strasbourg.

⁵ These accelerations were kindly communicated by O.Richard.

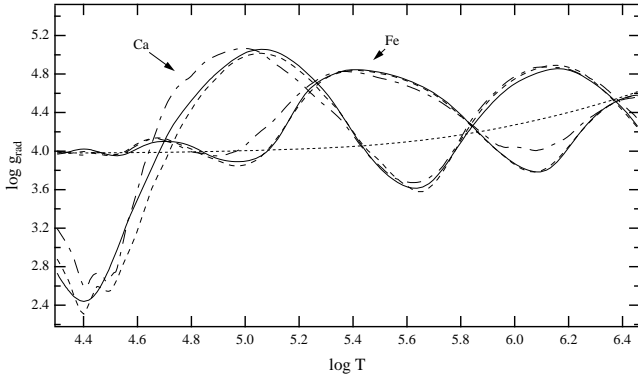


Fig. 2. Radiative accelerations of Ca and Fe using solar abundances calculated with the SVP method (solid lines) and those of Seaton (1997) (dashed lines) in the same stellar model as in Fig. 1. The dashed-dotted lines represent the accelerations from the models of Talon, Richard & Michaud (2006) using the local abundances obtained by the diffusion process. The local gravity is represented by the dotted curve.

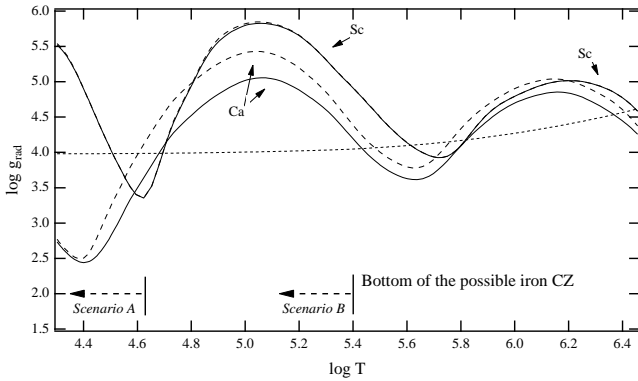


Fig. 3. Radiative accelerations of Ca and Sc for abundances of 1 (solid lines) and 0.1 (dashed lines) times their solar values in the same stellar model as in Fig. 1. The Sc accelerations are calculated by our interpolation method and those of Ca by the SVP method. Also shown are the approximate locations of the bottom of the convection zones of *scenarios A* and *B*, and the local gravity (dotted line).

to the Ar-like and Ne-like configurations, where the g_{rad} are naturally weaker. We can observe that the two curves for Sc are quite similar because this element is not very abundant and, at the abundances used here, the g_{rad} are completely unsaturated and near their maximal values.

Generally, we consider that the SVP method has an accuracy of about 30% (or 0.1 dex) compared to detailed methods in the temperature range of interest here (Paper II). We can suppose that the accuracy is of the same order of magnitude for our g_{rad} estimation for Sc. Unlike the curve shown for Ca in Fig. 1, the g_{rad} of Sc at low temperatures does not seem to have abnormal behaviour. This probably means that these g_{rad} are relatively good

throughout the model. However, only detailed g_{rad} calculations could confirm this.

3. The relative abundances of Ca and Sc in Am stars

The principal characteristic of Am stars is the presence of Ca and Sc deficiencies at their surface. Several observational studies have evaluated the abundances for these two elements as well as others in Am stars (e.g. Adelman 1994, Hui-Bon-Hoa, Burkhart & Alecian 1997, Hui-Bon-Hoa & Alecian 1998, Hui-Bon-Hoa 1999, Griffin 2002). These studies show that generally, Sc is more underabundant (relative to solar values) than Ca in Am stars.

When neglecting all other factors than gravity and radiative acceleration, if $g_{\text{rad}} > g$ the element will be driven upwards. While if $g_{\text{rad}} < g$ the element will migrate towards the centre of the star. At first approximation, since $g_{\text{rad}} > g$ means also that a larger abundance of the element can be supported by the radiation field, one considers that the element should become overabundant (with respect to solar value) in those layers, and underabundant in layers where $g_{\text{rad}} < g$. Of course, time-dependent diffusion, which is a non-linear process, is more complicated than what is described by this simplified approach.

As mentioned previously, two possible scenarios are suggested to explain these underabundances which both depend on the diffusion process.

Scenario A supposes that the surface abundances emanate from the regions below the superficial hydrogen convection zone, assuming a global mass flow (defined by the mass loss rate). These regions are near where the Ar-like configurations of Sc and Ca dominate, thus explaining their underabundance. Alecian (1986, 1996) showed that models with diffusion while including mass loss, can mimic a deepening of the surface mixing zone, and results in varying superficial abundances as a function of time. This study showed that the surface abundance of Ca and Sc for Am stars depend on both the mass loss rate and mixing length of convection. Time variation of superficial abundances due to mass loss was first considered qualitatively by Michaud & Charland (1986). They used a kinematic method and have shown that mass loss can produce variations of superficial abundances. But they have not solved the time-dependent continuity equation as in Alecian (1996). Both of these models do not take into account the structural changes due to diffusion as those of Richard, Michaud & Richer (2001) for instance.

Scenario B supposes that the surface abundances come from much deeper in the star, near where Sc and Ca are in the Ne-like configuration (Richard, Michaud & Richer 2001, Richer, Michaud & Turcotte 2000). A convection zone created by an accumulation of iron in the region where $\log T \simeq 5.3$ in these evolutionary models including atomic diffusion (but while neglecting mass loss) is at the base of this conclusion. The g_{rad} of Fe shown in Fig. 2 are consistent with an accumulation of this element in this region of the star. However, as previously mentioned, mass

loss could modify the stratification profiles of Fe and of the other elements.

More recently (Michaud, Richer & Richard 2005), these models were applied to the star *o* Leo A, and lead to similar abundances as observed by Griffin (2002) for this star. These authors mentioned that this star serves as a severe test for the deep mixing framework (*scenario B*). They also mention that a model supposing surface abundances created below the superficial hydrogen convection zone (Watson 1971) would be diluted during the subgiant phase. This point will be discussed in the conclusion. They also state that other species that could be compared to observations would be useful.

In Figure 3, we notice that in the region of the Ne-like configurations for Ca and Sc and where the abundance anomalies occur in *scenario B* (at $\log T \simeq 5.3$), the g_{rad} of Sc are larger than those of Ca, and even larger than gravity up to $\log T \simeq 5.6$. It is instructive to look at the curves with an abundance of 0.1 times solar values in Fig. 3, since in Am stars, both Ca and Sc are generally underabundant. These curves show that if *scenario B* is the correct one, the mixing has to be deeper than $\log T = 5.7$ for Sc to be more underabundant than Ca (relative to solar values). This is deeper than the mixing predicted in the models of Richard, Michaud & Richer (2001).

In the stellar model presented here, the bottom of the hydrogen convection zone is located at $\log T = 4.3$. This is not deep enough to explain the relative underabundances of Ca and Sc simultaneously, if one strictly considers the original model of Watson (1971). But, this is not incompatible with *Scenario A*. The region where the g_{rad} of Sc is weaker than those of Ca and that is consistent with their observed relative abundances is located near $\log T = 4.6$ for abundances of 0.1 times solar values. In this region, g_{rad} of both Ca and Sc are weaker than gravity for solar abundances. According to numerical modelling of a star not very far from the present situation, Alecian (1996) showed that, assuming mass loss and considering that the bottom of the mixing zone is uncertain, *Scenario A* could account for such simultaneous underabundances. However, only detailed evolutionary calculations while including diffusion will be able to determine which of the two scenarios is correct.

4. Conclusion

The radiative accelerations of Sc presented here shed new light on the source of Am stars' abundance anomalies and represents a new diagnostic tool to test various theoretical models. Scandium could be a key element to better understanding these stars.

Our results rekindle the question as to where the abundance anomalies emanate from in Am stars: either from a superficial or a much deeper mixing zone. The results shown here regarding g_{rad} of Sc suggest that for *scenario B* to be able to reproduce both the observed Ca and Sc abundances, the mixing must be deeper than that found in the models of Talon, Richard & Michaud (2006) or

those of Richard, Michaud & Richer (2001) for instance. In these models, the mixing goes down to approximately $\log T = 5.3$, while from the results shown here, it has to go down to approximately $\log T = 5.7$ to be able to reproduce both Ca and Sc observed abundances.

Relating to the question of dilution of the abundances during the subgiant phase of evolution, it is not clear if this argument can eliminate *scenario A*. Even though the surface underabundances are created at much shallower regions of the star in this scenario compared to *scenario B*, there should also exist an underabundance of both Ca and Sc in the two regions where the noble gas configurations dominate. The value of the overabundance that should prevail between these two regions as well as the depth of the mixing zone will determine to what extent the surface abundances are affected at the subgiant stage. Only detailed evolutionary calculations while including the deeper mixing at the subgiant stage could show how the surface abundances of *scenario A* are affected at that stage of evolution. The predicted abundances of other elements should also give insight into the amplitude of the dilution.

Our results show that near $\log T = 4.6$ (for abundances of 0.1 times solar values), the g_{rad} of Ca are stronger than those of Sc. *Scenario A* could then produce Ca and Sc abundances consistent with their relative observed abundances in Am stars. The results presented here for Sc thus reinforce the superficial mixing zone scenario but only evolutionary stellar models with mass loss and diffusion, while including Sc, might help to finally solve the Am stars' mysteries. We hope that the g_{rad} of Sc shown here, or others calculated directly from reliable atomic data, will be included in evolutionary models in the near future. For that purpose, the parameters for Sc calculated here are made available at <http://www.umoncton.ca/leblanfn/grad>.

Acknowledgements. Authors thank O. Richard for kindly communicating the stellar model used in this paper. This research was partially funded by NSERC and La Faculté des Études Supérieures et de la Recherche de l'Université de Moncton. We also thank RQCHP for computing time. One of us (FL) is grateful for a one month visiting position at l'Observatoire de Meudon and at l'Université de Paris 7. We acknowledge the financial support of Programme National de Physique Stellaire (PNPS) of CNRS/INSU, France.

References

- Abt, H. A. 1961, ApJS, 6, 37
- Adelman, S. J. 1994, MNRAS, 271, 355
- Alecian, G. 1985, A&A, 145, 275
- Alecian, G. 1986, A&A, 168, 204
- Alecian, G. & Artru, M.-C. 1990a, A&A, 234, 323
- Alecian, G. & Artru, M.-C. 1990b, A&AS, 83, 379
- Alecian, G. 1994, A&A, 289, 885
- Alecian, G. 1996, A&A, 310, 872
- Alecian, G. & LeBlanc, F. 2000, MNRAS, 319, 677
- Alecian, G. & LeBlanc, F. 2002, MNRAS, 332, 891 (Paper I)
- Griffin, R. E. 2002, AJ, 123, 988

- Hui-Bon-Hoa, A., Burkhart, & Alecian, G. 1997, A&A, 323, 901
- Hui-Bon-Hoa, A. & Alecian, G. 1998, A&A, 332, 224
- Hui-Bon-Hoa, A. 1999, A&A, 343, 261
- Kurucz, R. L. 1990, Trans. IAU, Vol. XXB, ed. McNally, D., (Kluwer), 168
- Kurucz, R. L. & Peytremann, E. 1975, Smithsonian Astrophys. Obs. Spce. Rep., 362
- LeBlanc, F., Michaud, G. & Richer, J. 2000, ApJ, 538, 876
- LeBlanc, F. & Alecian, G. 2004, MNRAS, 352, 1329 (Paper II)
- Michaud, G. 1970, ApJ, 160, 641
- Michaud, G., Tarasick, D., Charland, Y. & Pelletier, C. 1983, ApJ, 269, 239
- Michaud, G. & Charland, Y. 1986, ApJ, 311, 326
- Michaud, G., Richer, J. & Richard, O. 2005, ApJ, 623, 442
- Preston, G. W. 1974, ARA&A, 12, 257
- Rogers, F. J. & Iglesias, C. A. 1992, ApJ, 401, 361
- Richard, O., Michaud, G. & Richer, J. 2001, ApJ, 558, 377
- Richer, J., Michaud, G. & Turcotte, S. 2000, ApJ, 529, 338
- Seaton, M. J. 1997, MNRAS, 289, 700
- Seaton, M. J., Zeippen, C. J., Tully, J. A., Pradham, A. K., Mendoza, C., Hibbert, A. & Berrington, K. A. 1992, Rev. Mex. Astron. Astrofis., 23, 19
- Smith, M. A. 1971, A&A, 11, 325
- Talon S., Richard, O. & Michaud, G. 2006, ApJ, 645, 634
- Watson, W. D. 1971, A&A, 13, 263